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# Electron density-of-states and the metal-insulator transition in LaH<sub>x</sub>

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#### Abstract

The temperature dependence of the Gd<sup>3+</sup> impurity ion spin relaxation rate,  $\tau_i^{-1}$ , in lanthanum hydrides, LaH<sub>x</sub> (2.0≤x≤3.0), probes the metal-insulator (MI) transition in this system. Because Gd<sup>3+</sup> is an S-state ion,  $\tau_i^{-1}$  depends on interaction with conduction electrons in the metallic state, resulting in Korringa-type behavior,  $\tau_i T = \text{constant}$ , and  $(\tau_i T)^{-1/2} \propto N(E_F)$ , the electronic density-of-states at the Fermi level. In the non-metallic state, weak phonon processes result in a temperature dependence,  $\tau_i^{-1} \propto T^n$ , with 3 < n < 5. The rate  $\tau_i^{-1}$  has been measured via the Gd<sup>3+</sup>-induced contribution,  $R_{1p}$ , to the proton spin-lattice relaxation rate,  $R_1$ , by comparing the measured rate in pure LaH<sub>x</sub> with that in LaH<sub>x</sub> containing controlled low levels of Gd. The results show that in the metallic state,  $N(E_F) \propto (2.91 - x)^{1/3}$ , consistent with earlier results based on the <sup>139</sup>La Knight shift which also support  $N(E_F) \propto (2.91 - x)^{1/3}$ . © 2002 Published by Elsevier B.V. All rights reserved.

Keywords: Metal-insulator transition; Lanthanum hydrides: electronic structure

## 1. Introduction

Previous NMR studies have traced the x-dependence of the electronic density-of-states (DOS) at the La sites in LaH<sub>x</sub> (2.0 $\leq x \leq$ 3.0) at temperatures above the metal-insulator (MI) and order-disorder (OD) transitions, i.e. at T > 250 K, via the <sup>139</sup>La Knight shift,  $K(^{139}La)$ , and at the hydrogen sites at temperatures below these transitions, i.e. at T < 250 K, via the conduction electron contribution  $R_{1e}$ to the proton spin-lattice relaxation rate,  $R_1$  [1,2]. These measurements are consistent with the DOS following nearly-free-electron-like behavior, i.e. decreasing approximately as  $(3-x)^{1/3}$ , as expected if the conduction electron density decreases linearly with increasing x. On the other hand, low-temperature measurements (T < 8 K) of the x-dependence of the specific heat parameter  $\gamma$  are consistent with the DOS decreasing approximately as (3 - x)[3]. A further magnetic resonance approach to probing the DOS and the MI transition is to measure the temperature dependence of the spin-lattice relaxation rate,  $\tau_{i}^{-1}$ , of Gd<sup>3</sup> impurity ions in LaH<sub>x</sub>. Because Gd<sup>3+</sup> is an S-state ion,  $\tau_i^{-1}$ depends on interaction with conduction electrons in the

metallic state, resulting in Korringa-type behavior,  $\tau_i T =$  constant, and  $(\tau_i T)^{-1/2} \propto N(E_F)$ , the DOS at the Fermi level as modified by the Stoner factor which includes exchange and correlation enhancement effects. In the nonmetallic state, phonon processes yield the temperature dependence,  $\tau_i^{-1} \propto T^n$ , with 3 < n < 5. The rate  $\tau_i^{-1}$  has been measured at temperatures and compositions (*x*-values) both below and above the MI transition via the Gd<sup>3+</sup>-induced contribution to the proton spin-lattice relaxation rate,  $R_1$ , by comparing the measured rate in LaH<sub>x</sub> containing controlled low levels, e.g. 25–300 ppm, of Gd with that in pure LaH<sub>x</sub>.

#### 2. Theoretical background

The proton spin-lattice relaxation rate,  $R_1$ , in metalhydrogen systems frequently results from three contributions [4],

$$R_1 = R_{1d} + R_{1e} + R_{1p} \tag{1}$$

Here,  $R_{1d}$  is the proton–proton dipolar relaxation rate;  $R_{1e}$  results from the coupling of the proton moment to the conduction electrons (the Korringa rate), and  $R_{1p}$  arises from the dipolar coupling between the proton moment and

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the fluctuating electronic moment of paramagnetic impurity ions.

The strength of the proton–impurity moment interaction is defined by  $\tau^{-1}(r) = Cr^{-6}$  where  $\tau^{-1}(r)$  is the relaxation rate that a single proton would have at a distance *r* from the ion. For powder samples, *C* is given by [5,6]

$$C = (2/5)(\gamma_{\rm p}\gamma_{\rm n}\hbar)^2 J(J+1) [\tau_{\rm i}/(1+\omega_{\rm o}^2\tau_{\rm i}^2) + 7\tau_{\rm i}/3(1+\omega_{\rm e}^2\tau_{\rm i}^2)]$$
(2)

where J,  $\gamma_{\rm p}$ ,  $\tau_{\rm i}$ , and  $\omega_{\rm e}$  are the angular momentum, gyromagnetic ratio, spin-lattice relaxation time and Larmor frequency of the ion, respectively, and  $\gamma_{\rm n}$  and  $\omega_{\rm o}$  are the corresponding quantities for the proton. The relative importance of direct relaxation characterized by C and that due to diffusion characterized by D (whether spin or atom) is described by the pseudopotential radius,  $\beta = (C/D)^{1/4}$ , which is the distance from the impurity at which the rate of diffusion to the impurity equals the relaxation rate at the impurity. A second important parameter in the low-temperature rigid-lattice regime is the spin-diffusion barrier radius, b, which is roughly the distance at which the magnetic field due to the ion equals the local nuclear dipolar field at a proton site in the lattice, and within which spin diffusion is inhibited [5,6]. In the atom diffusion regime, b is replaced by the proton spin-ion spin nearestneighbor spacing  $a_1$ . Finally, the relative significance of b (or  $a_1$ ) and  $\beta$  is expressed by the parameter  $\delta = \beta^2/2b^2 =$  $(C/D)^{1/2}/2b^2$ . The general form for the relaxation rate is then [5,6]

$$R_{1p} = 8\pi ND\beta [\Gamma(3/4)/\Gamma(1/4)] [I_{3/4}(\delta)/I_{-3/4}(\delta)]$$
(3)

Here the  $I_{\rm m}(\delta)$  are the modified Bessel functions of fractional order, and *N* is the number density of impurity ions. This result applies to both spin and atom diffusion, i.e.  $D_{\rm s}$  or  $D_{\rm a}$ , with the limiting forms appropriate to the fast and slow diffusion regimes, i.e. weak and strong collision regimes, determined by  $\delta$ . Approximately,  $\delta \ge 2$  or  $\beta \ge 2b$ , defines the strong collision regime, and  $\delta \le 0.3$  or  $\beta \le 0.8b$  defines the weak collision regime. We focus here on the behavior of  $R_{\rm 1p}$  in the low-temperature spin-diffusion and high-temperature atom-diffusion regimes, which span the MI transition, and which are most amenable to quantitative interpretation.

### 3. Experimental aspects

All of the lanthanum hydride samples were prepared in the Materials Preparation Center of the Ames Laboratory from the highest purity lanthanum metal available. Details of their preparation were given previously in Ref. [2]. The pure (undoped) samples are those that were used in previous studies of the proton spin-lattice relaxation rate and <sup>139</sup>La Knight shift [2] and of hydrogen diffusivity [7]. The magnetic resonance instrumentation was also described in detail in Ref. [6]. All of the measurements reported here were made at a resonance frequency of 40 MHz.

The procedure followed has been to measure the temperature dependence of the proton  $R_1$  in pure LaH<sub>x</sub> and in the same composition containing a controlled low level of Gd impurity. For the low impurity levels involved, never greater than 300 ppm, there is no evidence that the  $R_{1d}$  and  $R_{1e}$  contributions in Eq. (1) differ in the two cases. Subtraction of the rate in the pure sample from that in the Gd-doped sample yields  $R_{1p}$ . The rate  $R_{1p}$  is a direct, linear function of the Gd content at least up to an impurity level of 1000 ppm.

All features of the Gd-induced spin-lattice relaxation are evident in the temperature dependence of  $R_{1p}$  for LaH<sub>2.61</sub>: 300 ppm Gd and LaH $_{2.60}$ : 25 ppm Gd shown in Fig. 1. This is the highest hydrogen concentration studied that shows unambiguous metallic character at both low and high temperatures. In addition, LaH<sub>~2.60</sub> shows only a negligible trace of the two-phase character evident at all higher x-values, which has been attributed to the accompanying OD transition [8]. At low temperatures, in the spin-diffusion regime,  $R_{1p}$  passes through a maximum when the condition  $\omega_{o}\tau_{i} \approx 1$  is satisfied. At approximately 150 K, atom diffusion becomes faster than spin diffusion, and  $R_{1p}$  increases exponentially. With further increasing temperature,  $R_{1p}$  passes through a second maximum at about 250 K when atom diffusion becomes sufficiently fast that multiple encounters with an impurity spin are required to relax the proton spin. This is the weak collision regime (fast atom diffusion regime) in which  $R_{1p}$  is independent of the atom diffusivity,  $D_a$ , but depends directly (or very nearly directly) on  $\tau_i$ .



Fig. 1. Temperature dependence of the Gd-induced spin-lattice relaxation rate,  $R_{1p}$ , in metallic LaH<sub>2.61</sub>: 300 ppm Gd (T < 130 K) and in metallic LaH<sub>2.60</sub>: 25 ppm Gd (T > 130 K). The solid curves through the low-temperature data points and the straight line through the high-temperature points are best fit results (see text). Measurements were made at a resonance frequency of 40 MHz.

## 3.1. Low temperatures (spin diffusion regime)

As noted above, in this limit for spin diffusion, an important feature results when  $\omega_o \tau_i \approx 1$ , which maximizes the first term in brackets in *C* [Eq. (2)], which enters Eq. (3) via the pseudo-potential radius  $\beta$ . The second term in brackets is negligible since  $(\omega_e \tau_i)^2 \gg 1$ . This condition creates a 'peak' in the temperature dependence of  $R_{1p}$ . The analysis is complicated, however, by the barrier radius *b* which also depends on  $\tau_i$  and by the parameter  $\delta$  which depends on  $\tau_i$  via both *b* and *C*. Assuming that  $\tau_i^{-1} \propto T^n$ , the low-temperature behavior can be fit to determine *n*. The solid curve through the low-temperature data points in Fig. 1 shows the fit with  $\tau_i^{-1} \propto T^{1.00}$  for LaH<sub>2.60</sub>: 300 ppm Gd.

#### 3.2. High temperatures (atom diffusion regime)

With increasing temperature, the atom diffusion rate exceeds that due to spin diffusion, and since the activation enthalpy,  $H_a$ , for hydrogen diffusion decreases rapidly with increasing x [7], the high-temperature  $R_{1p}$  maximum shifts progressively to lower temperatures. At the same time, the maximum value of  $R_{1p}$  increases sharply as the Gd<sup>3+</sup> spin relaxation rate,  $\tau_{i}^{-1}$ , slows down with decreasing metallic character, reflecting the decreasing electron DOS. These features are evident in Fig. 2 which shows the temperature dependence of  $R_{1p}$  due to 25 ppm Gd in LaH<sub>x</sub>, x = 2.00, 2.25, 2.60, and 3.00. The temperature at which the maximum occurs shifts from 500 K at x = 2.00 to 250 K at x=2.60 and 3.00, and the maximum  $R_{1p}$  increases by a factor of 80 between x = 2.00 and x = 3.00—indeed, by a factor of ~18 between 2.60 and 3.00. Fig. 2 also shows, for x = 3.00, the temperature range in which two proton



Fig. 2. Temperature dependence of the Gd-induced rate  $R_{1p}$  in LaH<sub>x</sub>, x=2.00, 2.25, 2.60, and 3.00, in the atom-diffusion regime. The rates shown have been standardized to an impurity concentration *N* of 25 ppm, based on the experimentally demonstrated linear dependence of  $R_{1p}$  on *N*. All measurements were made at a resonance frequency of 40 MHz.

resonances occur in both the pure and Gd-doped samples. These have been identified as arising from the ordered (low-temperature) and disordered (high-temperature) phases [8], and appear for  $x \ge 2.70$ .

In the fast atom diffusion (weak collision) limit ( $\beta < a_1$ ), many encounters are needed to yield relaxation, and  $R_{1p}$ becomes independent of  $D_a$ . In this limit, Eq. (3) becomes [9]

$$R_{1p} = \beta_0 N C / a_0^3 \tag{4}$$

Here  $a_0$  is the cubic lattice parameter, and  $\beta_0$  is a latticespecific sum over impurity ion sites, i.e.  $\beta_0 = (64/Z)\Sigma_i \rho_i^{-6}$ , where Z is the number of lattice sites per cubic cell. However, at high temperatures, the mean dwell time for diffusive hopping,  $\tau_D$ , may become short enough that  $\tau_D^{-1}$  becomes comparable to or greater than  $\tau_i^{-1}$ . In this case,  $\tau_i$  in Eq. (2) is replaced by  $\tau^{*-1} = \tau_i^{-1} + \tau_D^{-1}$ , and consequently reliable, independent values of  $\tau_D$  and its temperature dependence are needed to obtain those of  $\tau_i$ . These measurements have recently been made [7], furnishing values for the temperature dependence of the diffusivity,  $D_a$ , and of the activation enthalpy for diffusion,  $H_a$ , for LaH<sub>x</sub>,  $2.0 \le x \le 3.0$ . Values of  $\tau_D$  are obtained from the relation,  $D_a = \langle L^2 \rangle / 6\tau_D$ , where L is the diffusive path length, shown in recent neutron diffraction studies [10] to be the T–O site spacing, 0.244 nm, at high x-values.

Now  $R_{1p}$  is determined by Eq. (4), with  $(\omega_o \tau^*)^2 \ll 1$ and  $(\omega_e \tau^*)^2 \gg 1$ , so that the first term in the square brackets in Eq. (2) becomes  $\tau^*$  and the second term is negligible, with the result that  $R_{1p} \propto \tau^*$ . The temperature dependence of  $R_{1p}$  yields that of  $\tau^*$ , and with knowledge of  $\tau_D$  the temperature dependence of  $\tau_i$  can be obtained. This is the procedure followed to analyze the high temperature measurements for x-values beginning with x =2.60.

#### 4. Results and discussion

#### 4.1. Metallic state

Results for the metallic state, in which  $\tau_i^{-1} \propto T$ , are shown in Fig. 3, where the low temperature, i.e. T < 250 K, measurements are indicated by squares and those for T >250 K, by circles. These show that LaH<sub>x</sub> remains metallic at low temperatures at least up to and including x = 2.80. This is consistent with resistivity results that show a transition from metallic to semiconducting behavior at  $T \approx 250$  K for x = 2.70, 2.80 and intermediate compositions up to 2.90 [11,12], but semiconducting only at x = 2.93[11]. In the present work, measurements at x = 2.90 failed to detect the low-temperature  $R_{1p}$  peak, probably because, if there is one, it occurs at  $T \approx 170$  K and is hidden by the sharp rise in  $R_{1p}$  when  $D_a > D_s$  (Fig. 1). For x = 2.60, the  $R_{1p}$  measurements show metallic behavior at both low and



Fig. 3. Dependence of  $(\tau_i T)^{-1/2}$  for Gd<sup>3+</sup> on hydrogen concentration, x=[H]/[La]. Circles are for measurements made at high temperatures (T > 250 K), and squares for those made at low temperatures (T < 250 K). The solid curve is the best fit of  $(\tau_i T)^{-1/2} \propto (x_c - x)^{1/3}$  to the data, with  $x_c = 2.91$ , and the dashed line shows (3-x) behavior.

high temperatures. Therefore, we conclude that  $LaH_x$  remains metallic at all temperatures for  $x \le 2.60$ , and at low temperatures for  $2.60 \le x \le 2.80$ .

The principal feature of Fig. 3 is the dependence of  $(\tau_i T)^{-1/2}$  on hydrogen concentration *x*. The solid curve shows the least-squares fit (regression coefficient r=0.997) for  $(\tau_i T)^{-1/2} \propto N(E_F) \propto (x_c - x)^{1/3}$ , which is the dependence expected if  $N(E_F)$  follows essentially rigid-band free-electron-like behavior, with the conduction electron density, *n*, decreasing linearly as *x* increases from 2 to  $x_c = 2.91$ , reflecting the withdrawal of electrons from the Fermi level to form a bonding band with O-site hydrogen atoms,  $x_c$  being the critical *x*-value. The dashed straight line in Fig. 3 shows the approximate dependence of the specific heat parameter  $\gamma$  on *x* [3]. Assuming that  $\gamma \propto N(0)$ , the 'bare' DOS, then these data imply  $N(0) \propto (3 - x)$ .

As noted earlier, NMR measurements of  $K(^{139}\text{La})$  at T > 250 K and of the proton  $R_{1e}$  at T < 250 K are also consistent with  $N(E_F) \propto (x_c - x)^{1/3}$  [1,2]. These measurements are shown in Fig. 4 (adapted from Fig. 1 of Ref. [2]). The solid curves are least-squares fits of  $(x_c - x)^{1/3}$  to the data points. It is significant that the fit curve for  $K(^{139}\text{La})$  also yields  $x_c = 2.91$ . In making this fit, the two data points at x = 2.92 and 2.99 have been excluded. These points show that the shift becomes constant at 0.118% at temperatures greater than 250 K, suggestive of a chemical



Fig. 4. Dependence of the proton  $(T/R_{1e})^{-1/2} = (T_{1e}T)^{-1/2}$  (a), and of  $K(^{139}\text{La})$  (b), on hydrogen concentration, x = [H]/[La], adapted from Ref. [2]. For  $K(^{139}\text{La})$  the circles are from Ref. [1], and the triangles are Ames Laboratory results. The proton  $(T_{1e}T)^{-1/2}$  data are Ames Laboratory results. The solid curves through the data points are least-squares fits of  $(x_e - x)^{1/3}$  with  $x_e = 2.91$  for  $K(^{139}\text{La})$  and 3.04 for the proton  $(T_{1e}T)^{-1/2}$ .

shift in the nonmetallic phase [2]. For  $T < T_{OD}$  the rapid increase in the <sup>139</sup>La resonance linewidth due to secondorder quadrupole broadening poses severe difficulties to measuring the Knight shift at low temperatures [13]. The proton  $(T_{1e}T)^{-1/2}$  results at high *x*-values may be unreliable due to the  $R_{1p}$  contribution from the residual rareearth impurity content, even though the samples were based on the highest available purity Ames Laboratory La metal. This could account for the fact that these data yield  $x_c = 3.04$ .

#### 4.2. Insulating (semiconducting) state

Following the data analysis procedure described above, and taking account of  $\tau_{\rm D}^{-1}$ , the high-temperature results for x = 2.70, 2.80, 2.90, and 3.00 conform to  $\tau_{\rm i}^{-1} \propto T^n$  behavior with  $n = 3.9 \pm 0.5$ . This is consistent with the Gd<sup>3+</sup> spin relaxation rate measured in insulating solids [14], and confirms the insulating (semiconducting) character of the high-temperature disordered phase for  $x \ge 2.70$ .

## 5. Conclusions

Measurements of the temperature dependence of the Gd<sup>3+</sup> spin-lattice relaxation rate in LaH<sub>x</sub>,  $2.00 \le x \le 3.00$ , support the following conclusions:

- 1. LaH<sub>x</sub> is metallic at all temperatures for  $x \le 2.60$ .
- 2. For 2.60  $\leq x \leq$  2.91, LaH<sub>x</sub> is metallic at low tempera-

tures and insulating (semiconducting) at high temperatures.

- 3. For  $x \ge 2.91$ , LaH<sub>x</sub> is insulating at all temperatures.
- 4. In the metallic state, whether at low or high temperatures, the electron DOS at the Fermi level,  $N(E_{\rm F})$ , follows rigid-band, free-electron-like behavior, i.e.  $N(E_{\rm F}) \propto (2.91 x)^{1/3}$ .

In addition, previous measurements [1,2] of  $K(^{139}$ La) also support the conclusion that  $N(E_F) \propto (2.91 - x)^{1/3}$  in the metallic state. The earlier  $K(^{139}$ La) results also indicate that LaH<sub>x</sub> is insulating (semiconducting) for  $x \ge 2.91$ , consistent with the present  $(\tau_i T)^{-1/2}$  results. Moreover, although the details of the dependence of the proton  $R_{1e}$ , of  $K(^{139}$ La), and of  $\tau_i^{-1}(\text{Gd}^{3+})$  on  $N(E_F)$  involve different effective hyperfine fields and/or exchange integrals and Stoner enhancement factors [4,15], the result is that all three NMR approaches yield essentially the same result at both low and high temperatures within the metallic state.

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